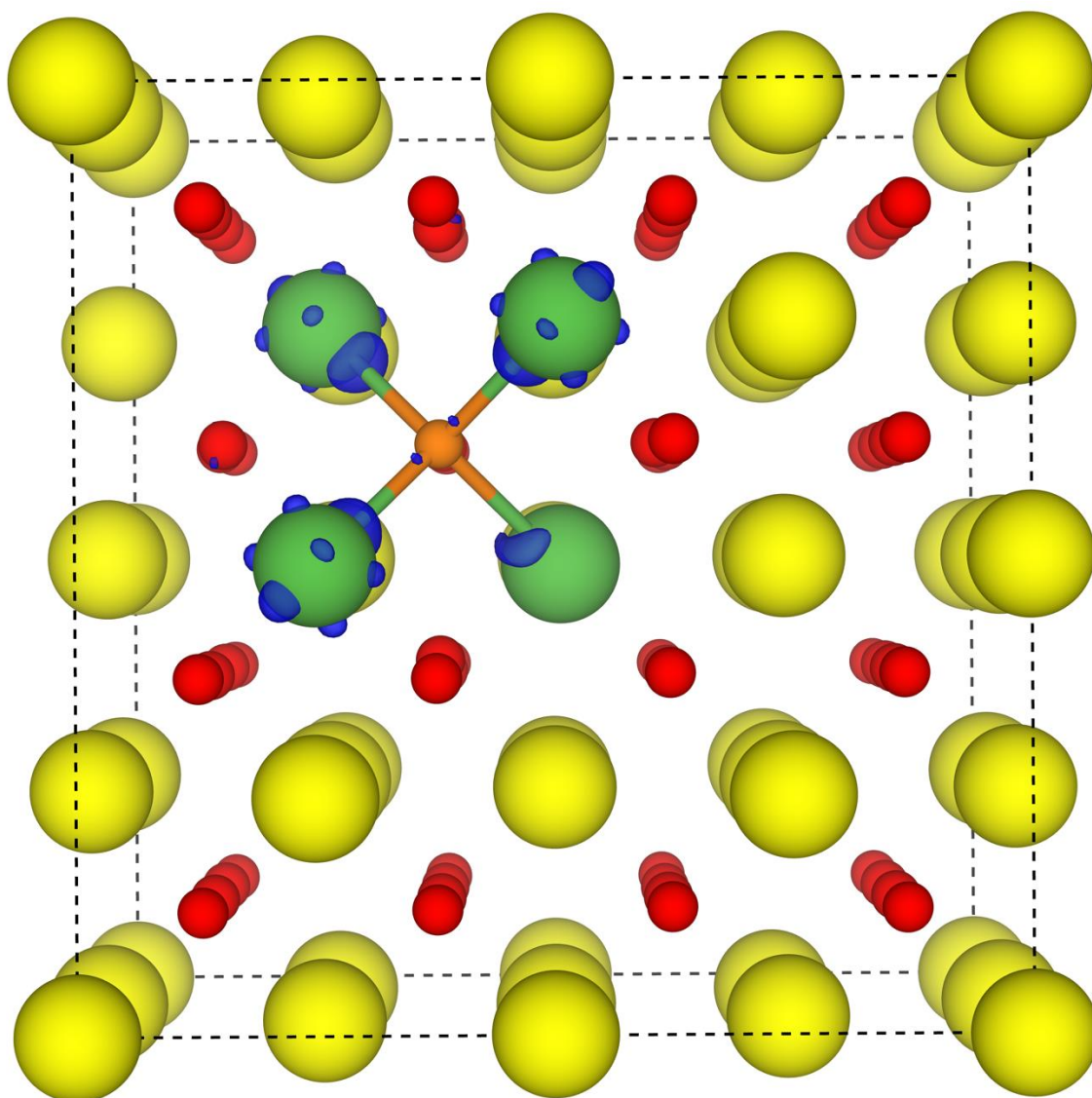


## Supporting Information

**A first-principles-based sub-lattice formalism for predicting off-stoichiometry in materials for solar thermochemical applications: the example of ceria**

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**Figure S1.** Difference in electron density between pure and defective CeO<sub>2</sub>. Yellow and red spheres respectively correspond to Ce and O ions, while the orange and green spheres respectively signify the oxygen vacancy (Va<sub>O</sub>) and Ce ions that are nearest neighbors (NN) to the Va<sub>O</sub>. Blue isosurfaces indicate regions of electron accumulation when a Va<sub>O</sub> is created, with the isosurface set to 0.009 e/bohr<sup>3</sup>. Thus, the electrons generated due to a Va<sub>O</sub> tend to reduce the NN Ce atoms, with some delocalization amongst the NN Ce, as highlighted by the presence of blue isosurfaces on all four NN Ce.

### **S1 Errors due to excluding temperature dependence when estimating the oxygen chemical potential**

The mathematical expression for the oxygen chemical potential ( $\mu_O$ ) in  $\text{CeO}_{2-\delta}$  can be derived by differentiating  $G_{\text{CeO}_x}^F$  in **Equation 23** in the main text with respect to  $\delta = 2 - x$ , and can be written as follows.

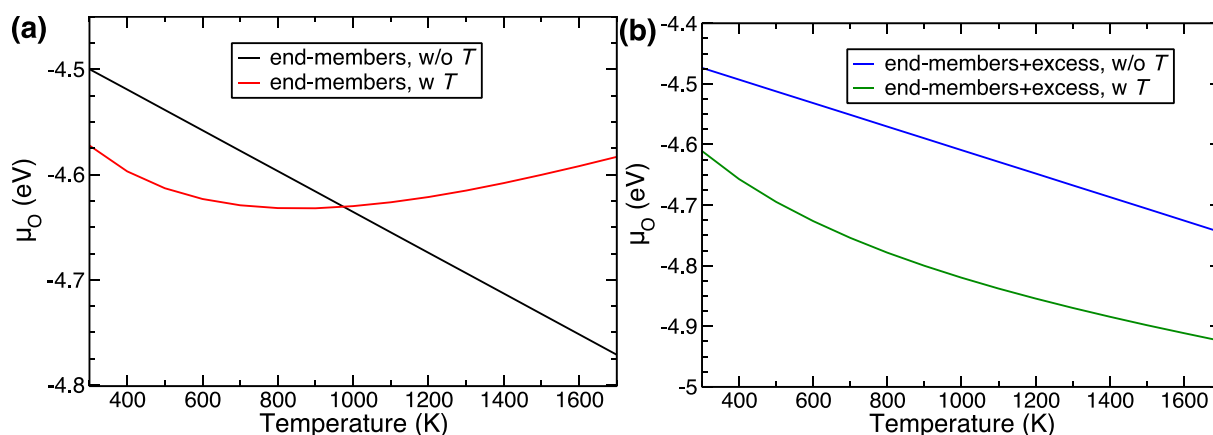
$$\mu_O = -\frac{dG_{\text{CeO}_{2-\delta}}^F}{d\delta} = 2[G_{\text{CeO}_2}^F - G_{\text{CeO}_{1.5}}^F] + 4RT \left\{ \frac{3}{4} \ln \frac{3}{4} + \frac{1}{4} \ln \frac{1}{4} \right\} + (8\delta - 2)(L_0 - L_1) + (48\delta^2 - 16\delta)L_1 - RT \left[ 2 \ln \left( \frac{2\delta}{1-2\delta} \right) + \ln \left( \frac{\delta}{2-\delta} \right) \right] \quad (\text{S1})$$

Thus,  $\mu_O$  in **Equation S1** can be split into three-components, namely,  $\mu_O^{\text{end-members}}$ ,  $\mu_O^{\text{excess}}$ ,  $\mu_O^S$ , which arise from  $G^{\text{end-members}}$ ,  $G^{\text{excess}}$ , and  $S^{\text{soln}}$ , respectively. Specifically, the expressions for the three  $\mu_O$  components are,

$$\begin{aligned} \mu_O^{\text{end-members}} &= 2[G_{\text{CeO}_2}^F - G_{\text{CeO}_{1.5}}^F] + 4RT \left\{ \frac{3}{4} \ln \frac{3}{4} + \frac{1}{4} \ln \frac{1}{4} \right\} \\ \mu_O^{\text{excess}} &= (8\delta - 2)(L_0 - L_1) + (48\delta^2 - 16\delta)L_1 \\ \mu_O^S &= -RT \left[ 2 \ln \left( \frac{2\delta}{1-2\delta} \right) + \ln \left( \frac{\delta}{2-\delta} \right) \right] \end{aligned} \quad (\text{S2})$$

While the  $\mu_O^S$  employed in this work is identical to the model of Zinkevich et al.,<sup>[67]</sup> we do not account for the temperature dependence of  $G_{\text{CeO}_2}^F$  and  $G_{\text{CeO}_{1.5}}^F$  in  $\mu_O^{\text{end-members}}$  and  $L_0$  and  $L_1$  in  $\mu_O^{\text{excess}}$ , which can contribute to discrepancies between the two models. To better quantify the sensitivity of the temperature-dependent contributions, we plot variation in  $\mu_O$  with temperature (from 300-1700 K) in **Figure S2**, with and without the temperature dependence of the end-member and excess terms. Specifically, we plot two distinct scenarios where we include only  $\mu_O^{\text{end-members}}$  (panel a in Figure S2), and  $\mu_O^{\text{end-members}} + \mu_O^{\text{excess}}$  (panel b). Since  $\mu_O^{\text{excess}}$  is dependent on  $\delta$ , we set  $\delta \rightarrow 0$  in Figure S2b. Additionally, the absolute values of all  $\mu_O$  components are calculated using the

values provided by Zinkevich et al.<sup>[67]</sup> to accurately quantify the errors due to excluding the temperature-dependence.



**Figure S2.** Variation of the oxygen chemical potential in  $\text{CeO}_{2-\delta}$  with temperature is plotted including only the end-member contributions (panel a), and end-member+excess components (panel b). The legends “w T” and “w/o T” indicate including and excluding the temperature-dependences of the end-member and excess terms.

Although  $\mu_{\text{O}}^{\text{end-members}}$  (in Figure S2a) displays qualitative differences between excluding (“w/o T”, black line), and including (“w T”, red curve) temperature dependence, the absolute differences between the two scenarios is quite low. For example, the maximum deviation w and w/o T in  $\mu_{\text{O}}^{\text{end-members}}$  is  $\sim 4\%$  (at 1700 K). However, adding the  $\mu_{\text{O}}^{\text{excess}}$  component (panel b) reduces the qualitative differences between w/o T and w T scenarios (both  $\mu_{\text{O}}$  decrease monotonically with temperature), with the magnitude of deviation ranging from 3% to 4.6%, signifying a similar magnitude of error across all temperatures.